

Chapter 8

8-1

Assuming that the 150 G.Lite subscribers have VF service over the DSL lines, as well as VF service to the 300 VF subscriber lines, we get

$$300 \times 64 \text{ kb/s} + 150 \times 64 \text{ kb/s} + 150 \times 1,500 \text{ kb/s} \\ = 253,800 \text{ kb/s} = \underline{253.8 \text{ Mb/s}}$$

8-7

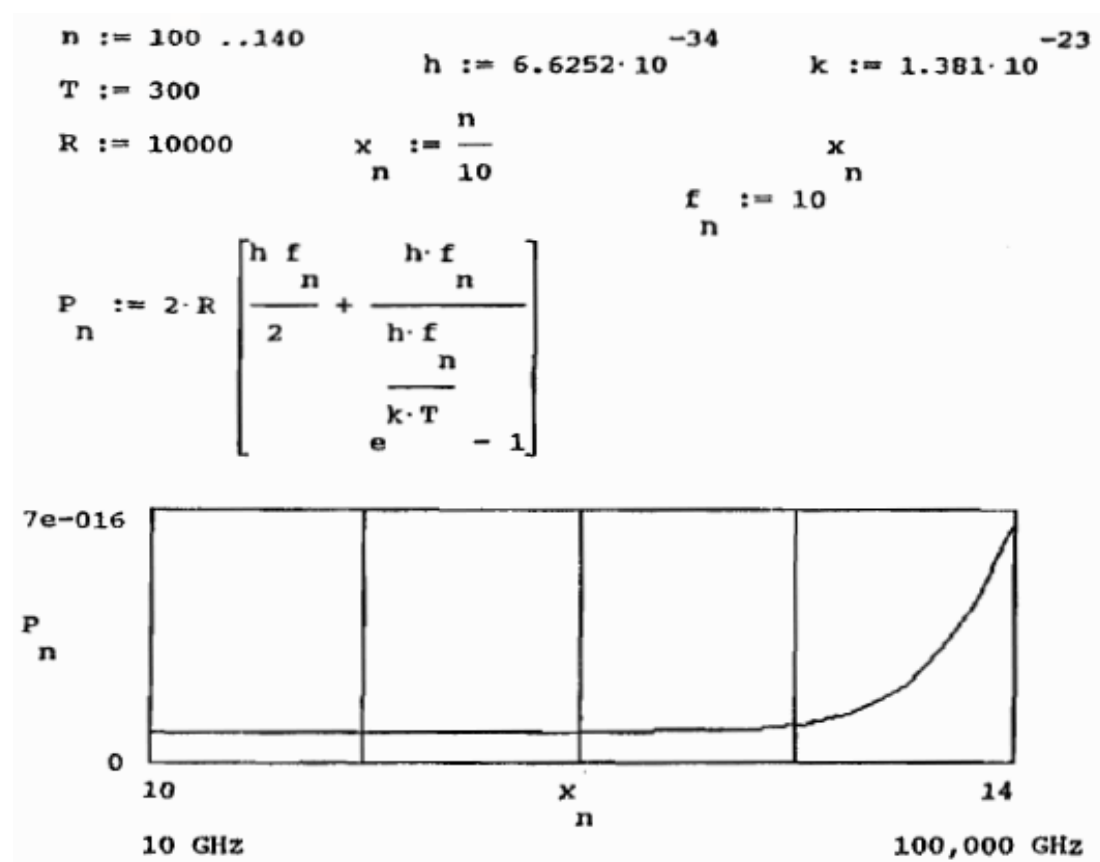
$P_{Tx} = 0.1 \text{ W}$, $f_c = 2 \text{ GHz}$, 3.28 ft/meter

(a.) $G_A = \frac{7A}{\lambda^2} \times \frac{7.0 \pi \left(\frac{3.28}{2}\right)^2}{\left(\frac{3 \times 10^8}{2 \times 10^9}\right)^2} = \underline{363.4} = \underline{25.6 \text{ dB}}$
 $A = \pi r^2$, $\lambda = c/f$ $10 \log(363.4) = 25.6$

(b.) $P_{EIRP} = P_{Tx} G_{AT} = 0.1 (363.4) = \underline{36.3 \text{ W}}$

(c.) $P_{Rx} = P_{Tx} G_{AT} G_{AR} \left(\frac{\lambda}{4\pi d}\right)^2 = (0.1)(363.4)^2 \left[\frac{(0.15)(3.28)}{4\pi(15)(5280)}\right]^2$
 $\Rightarrow P_{Rx} = 3.23 \times 10^{-9} \text{ W}$
 or $(P_{Rx})_{\text{dBm}} = 10 \log \left(\frac{3.23 \times 10^{-9}}{10^{-3}} \right) = \underline{-54.9 \text{ dBm}}$

8-8



8-13

(a.) $T_{\text{eff}} = T_0 (F - 1)$
 $= 290 (10^{.16} - 1) = \underline{\underline{129^\circ \text{K}}}$

(b.) $P_{a_{\text{out}}} = k T_{\text{IN}} B G_a$
 $= (1.38 \times 10^{-23}) (30^\circ + 129^\circ) (10 \times 10^6) (10^3)$
 $= \underline{\underline{2.2 \times 10^{-11} \text{ W}}}$
 $= 10 \log_{10} \left(\frac{2.2 \times 10^{-11}}{10^{-3}} \right) = \underline{\underline{-76.6 \text{ dBm}}}$

8-15

From Table 7-1 for FSK w/ incoherent detection:

$$p_e = \frac{1}{2} e^{-\frac{1}{2}(E_b/N_{total})}$$

$$N_{total} = k(T_0 + T_{eff}) = k(T_0 + (F-1)T_0) = kFT_0$$

$$T_{eff} = (F-1)T_0$$

$$= (1.38 \times 10^{-23}) (10^{6/10}) (290)$$

$$\frac{E_b}{N_{total}} = \frac{P_s T}{N_{total}} = \frac{P_s}{N_{total} R} = \frac{V_s^2 / R_n}{k F T_0 R} = 28.53$$

$$p_e = \frac{1}{2} e^{-\frac{1}{2}(28.53)} = \underline{\underline{3.2 \times 10^{-7}}}$$

8-20

Diagram of a two-stage system:

Handwritten equations for system noise temperature:

$$T_{sys} = T_A + T_e = T_A + \left(T_{e1} + \frac{T_{e2}}{G_1} \right) = T_A + \left(T_{e1} + T_{e2} L_1 \right)$$

$$\Rightarrow T_{sys} = T_A + \underbrace{\left[T_o(L_1 - 1) + T_{e2} L_1 \right]}_{T_e}. \text{ Also } T_e = T_o(F - 1) \Rightarrow F = \frac{T_e}{T_o} + 1$$

(a) Compute the system noise temperature T_s evaluated at the antenna input of the waveguide:

Parameters:

- $T_A := 160 \text{ K}$
- $T_o := 290 \text{ K}$
- $T_{e2} := 800 \text{ K}$
- $L_1 := 10^{0.2}$
- $G := 10^{12}$
- $B := 10^6 \text{ Hz}$

Calculations:

$$T_e := T_o \cdot (L_1 - 1) + T_{e2} L_1$$

$$T_s := T_A + T_e$$

$$\underline{\underline{T_s = 1597.534 \text{ K}}}$$

(b) Noise figure F :

$$F := \frac{T_e}{T_o} + 1$$

$$\underline{\underline{F = 5.957}}$$

$$\text{FdB} := 10 \cdot \log(F)$$

$$\underline{\underline{\text{FdB} = 7.75}}$$

(c) The available output noise power P_{no} :

$$P_{no} := 1.38 \cdot 10^{-23} \cdot T_s \cdot B \cdot G$$

$$\underline{\underline{P_{no} = 0.022 \text{ Watt}}}$$

8-22

Assume 4 GHz down link

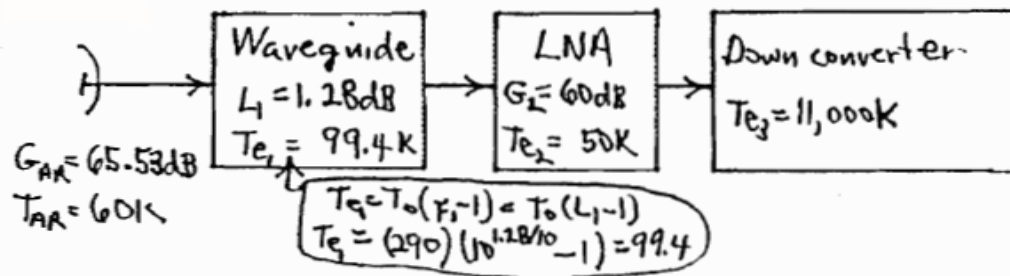
$$\frac{G_{AR}}{T_{sys}} = 10^4 = \frac{4\pi\eta [\pi(15)^2]}{85 \left(\frac{3 \times 10^8}{4 \times 10^9} \right)^2} = 1.86 \times 10^4 \eta$$

$$\Rightarrow \underline{\underline{\eta = 54\%}} \text{ for 30m antenna}$$

$$10^4 = 1.86 \times 10^4 \eta \left[\frac{(12.5)^2}{(15)^2} \right] = 1.29 \times 10^4 \eta$$

$$\Rightarrow \underline{\underline{\eta = 77.4\%}} \text{ for 25m antenna}$$

8-25



$$(a.) T_s = (T_{AR} + T_{e1}) G_1 + \left(T_{e2} + \frac{T_{e3}}{G_2} \right) = \frac{T_{AR} + T_{e1}}{L_1} + \left(T_{e2} + \frac{T_{e3}}{G_2} \right)$$

$$G_s = G_{AR} G_1 = \frac{G_{AR}}{L_1}$$

$$(b.) T_s = T_{AR} + T_e = T_{AR} + \left(T_{e1} + \frac{T_{e2}}{G_1} + \frac{T_{e3}}{G_1 G_2} \right)$$

$$\neq T_s = T_{AR} + \left(T_{e1} + T_{e2} L_1 + T_{e3} \frac{L_1}{G_2} \right)$$

$$G_s = G_{AR}$$

$$(c.) T_s = (T_{AR} + T_{e1}) G_1 G_2 + T_{e2} G_2 + T_{e3} = (T_{AR} + T_{e1}) \frac{G_2}{L_1} + T_{e2} G_2 + T_{e3}$$

$$G_s = G_{AR} G_1 G_2 = \frac{G_{AR} G_2}{L_1}$$

$$G_{AR} := 10^{\frac{65.53}{10}}$$

$$L_1 := 10^{\frac{1.28}{10}}$$

$$G_2 := 10^{\frac{60}{10}}$$

$$T_{e3} := 11000$$

$$T_{AR} := 60$$

$$T_{e1} := 290 \cdot (L_1 - 1)$$

$$T_{e2} := 50$$

$$(a.) T_s := \frac{T_{AR} + T_{e1}}{L_1} + T_{e2} + \frac{T_{e3}}{G_2}$$

$$T_s = 168.723$$

$$G_s := \frac{G_{AR}}{L_1}$$

$$G_s = 2.661 \cdot 10^6$$

$$GT_{\text{dB}} := 10 \cdot \log \left(\frac{G_s}{T_s} \right)$$

$$GT_{\text{dB}} = 41.978$$

(b.)

$$T_s := T_{AR} + T_{e1} + T_{e2} \cdot L_1 + T_{e3} \cdot \frac{L_1}{G_2}$$

$$T_s = 226.555$$

$$G_s := G_{AR}$$

$$G_s = 3.573 \cdot 10^6$$

$$GT_{\text{dB}} := 10 \cdot \log \left(\frac{G_s}{T_s} \right)$$

$$GT_{\text{dB}} = 41.978$$

(c.)

$$T_s := (T_{AR} + T_{e1}) \cdot \frac{G_2}{L_1} + T_{e2} \cdot G_2 + T_{e3}$$

$$T_s = 1.687 \cdot 10^8$$

$$G_s := G_{AR} \cdot \frac{G_2}{L_1}$$

$$G_s = 2.661 \cdot 10^{12}$$

$$GT_{\text{dB}} := 10 \cdot \log \left(\frac{G_s}{T_s} \right)$$

$$GT_{\text{dB}} = 41.978$$

8-27

$$f_c = 2 \text{ GHz} ; \lambda = \frac{c}{f} = \frac{3 \times 10^8}{2 \times 10^9} = .15 \text{ m}$$

$$\frac{E_b}{N_0} = \frac{P_{TX} G_{AT} G_{FS} G_{AR}}{K T_{sys} R}$$

$$G_{AT} = \frac{E_b}{N_0} \frac{K T_{sys} R}{P_{TX} G_{FS} G_{AR}}$$

$$G_{FS} = \left(\frac{\lambda}{4\pi d} \right)^2 \cdot L_{incidental} = \left(\frac{0.15}{4\pi (7.5 \times 10^2)} \right)^2 (10^{-0.2}) = 1.6 \times 10^{-30}$$

$$G_{AR} = 7\pi \left(\frac{r}{\lambda} \right)^2 = 7\pi \left(\frac{32}{0.15} \right)^2 = 1 \times 10^6$$

$$G_{AT} = \frac{10^{0.988} (1.38 \times 10^{-23}) (16) (300)}{10 (1.6 \times 10^{-30}) (10^6)} = 4.03 \times 10^4 = \frac{7A}{\lambda^2} = \frac{7A}{(0.15)^2}$$

(parabolic) $\rightarrow \lambda^2$

$$\Rightarrow A = 129.44 \text{ m}^2 = \pi r^2$$

$$\pm r = \sqrt{\frac{129.44}{\pi}} = 6.42 \text{ m} \Rightarrow \underline{\underline{D = 2r = 12.84 \text{ m}}} \text{ parabolic ant (rather large)}$$

8-29

Using (8-47) and (8-8)

$$P_{dBm}(d) = P_{dBm}(d_0) - 10n \log \left(\frac{d}{d_0} \right)$$

where $P_{dBm}(d_0) = (P_T)_{dBm} + (G_{TA})_{dBm} - 20 \log \left(\frac{4\pi d_0}{\lambda} \right) + (G_{AR})_{dBm}$

$$= 40 + 18 - 20 \log \left(\frac{4\pi (0.25 \text{ miles}) (5280 \text{ ft/mile}) \left(\frac{1 \text{ m}}{3.28 \text{ ft}} \right)}{3 \times 10^8 / 1.8 \times 10^9} \right) + 0$$

$\Rightarrow P_{dBm}(d_0) = -31.64 \text{ dBm}$ $\rightarrow 89.64$

Distance (miles)	Power Received (dBm)				
	0.25	1	2	5	10
$n=2$ (free space)	-31.6	-43.7	-49.7	-57.7	-63.7
$n=3$	-31.6	-49.7	-58.7	-70.6	-79.7
$n=4$	-31.6	-55.7	-67.8	-83.7	-95.7

8-32

The available bandwidth is

$$B_T = \frac{1}{2} f_h = \frac{1}{2} (15.734) = 7.867 \text{ kHz}$$

Referring to Fig. 8-33, the spectrum of the professional subcarrier (PSC) needs to roll off fast enough so that it does not interfere with the SAP FM subcarrier and the DSB-SC stereo subcarrier. Since the SAP subcarrier is FM, the capture effect of the FM detector will suppress the PSC interference when the PSC spectrum is, say, 10 to 15 dB below the SAP spectrum (in the SAP band). Referring to Fig. 5-33, it is seen that these interference specifications are easily satisfied if the first-null bandwidth criterion is used. Thus, for the M-ary signal class,

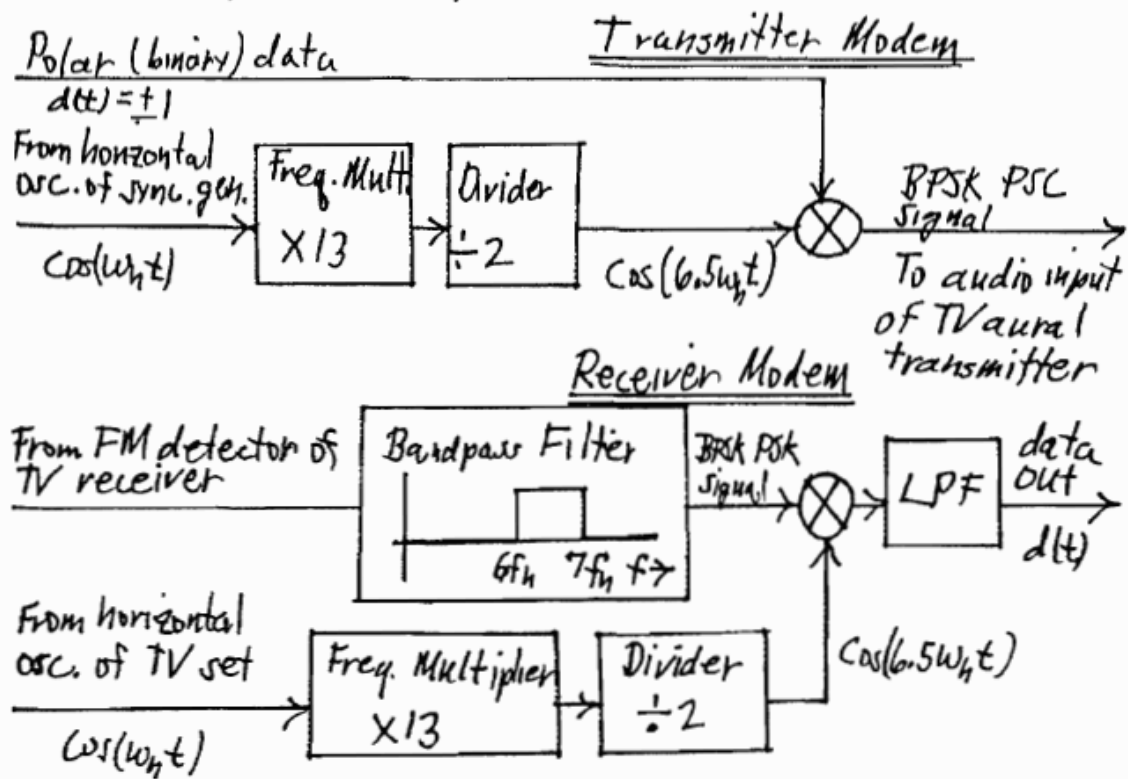
8-32 (Continued)

$$B_T = 2 \left(\frac{R}{\ell} \right) \leq 7.867 \text{ or } \ell \geq \left(\frac{2R}{7.867} \right)$$

(a) For $R = 1.2 \text{ kb/s}$, $\ell \geq \left(\frac{2(1.2)}{7.867} \right) = 0.305$.

\Rightarrow Choose $\ell = 1 \Rightarrow$ Use BPSK signaling

A $R = 1200 \text{ b/s}$ BPSK system is shown below.



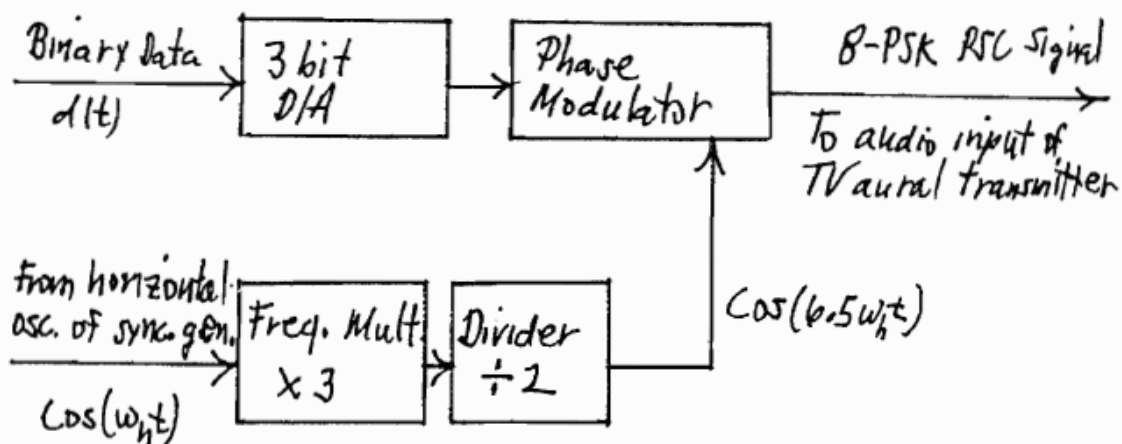
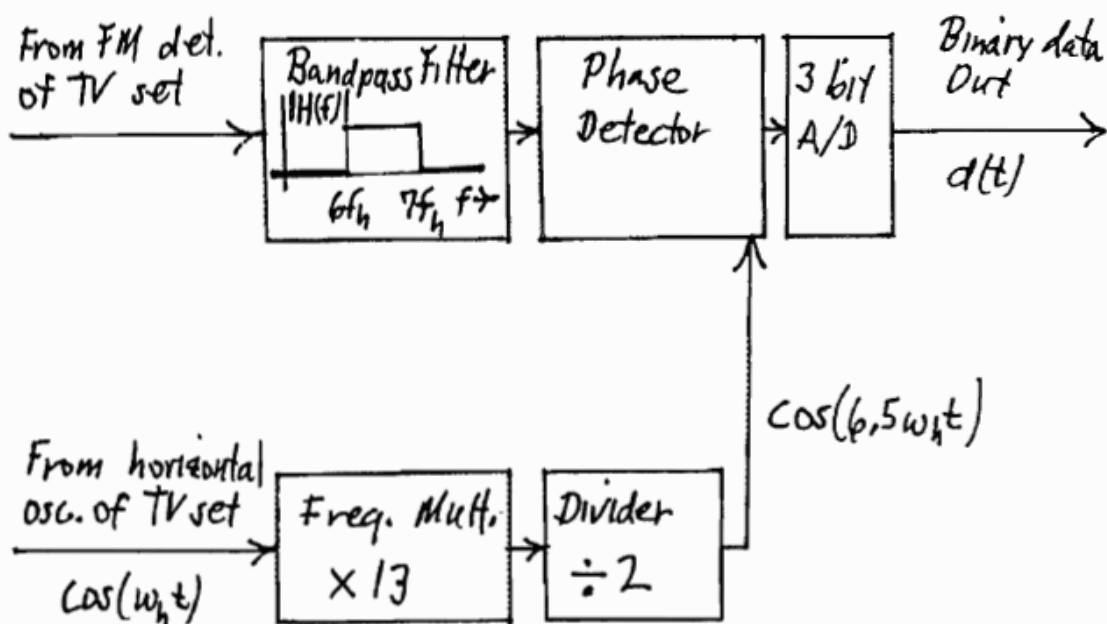
(b) For $R = 9.6 \text{ kb/s}$, $\ell \geq \left(\frac{2(9.6)}{7.867} \right) = 2.44$

\Rightarrow Choose $\ell = 3 \Rightarrow M = 2^3 = 8$

\Rightarrow Use 8-PSK

8-32 (Continued)

A $R=9600$ b/s 8-PSK system is shown below

Transmitter ModemReceiver Modem

8-34

$$R_{\text{with Coding}} = (R_{\text{without coding}}) \left(\frac{1}{R_{\text{TCM}}} \right) \left(\frac{1}{R_{\text{RS}}} \right) = 19.39 \left(\frac{3}{2} \right) \left(\frac{207}{187} \right)$$

$$\Rightarrow R_{\text{with Coding}} = 32.20 \text{ Mb/s}$$

$$\Rightarrow D_{\text{with coding}} = \frac{R_{\text{with coding}}}{l} = \frac{32.2}{3} = 10.73 \text{ Mbaud}$$

$(l=3 \text{ for } 8 \text{ levels})$

The segment sync replaces the payload sync at the beginning of each segment. One segment of training data is added after 312 segments.

Thus,

$$D_{\text{overall}} = (D_{\text{with coding}}) \left(\frac{312+1}{312} \right) = 10.73 \left(\frac{312+1}{312} \right) = \underline{\underline{10.76 \text{ Mbaud}}}$$

Appendix B

B-1

$$P(1) = \frac{n_1}{N} = \frac{1428}{1428 + 2668} = \underline{\underline{0.3486}}$$

B-3

$$(a.) P(1+3+5) = P(1) + P(3) + P(5) = \frac{3}{6} = \underline{\underline{\frac{1}{2}}}$$

$$(b.) P(4/E) = \frac{P(4 \cdot E)}{P(E)} = \frac{P(4)}{P(E)} = \frac{1/6}{1/2} = \underline{\underline{\frac{1}{3}}}$$

B-8

$$(a.) \int_{-\infty}^{\infty} f(x) dx = 1 = \int_0^{\infty} k e^{-bx} dx$$

$$= \frac{k e^{-bx}}{-b} \Big|_0^{\infty} = \frac{k}{b} [e^{-\infty} - e^0] = \frac{k}{b} = 1 \Rightarrow \underline{\underline{k=b}}$$

$$(b.) f(x) = b e^{-bx}$$

$$m = \bar{x} = \int_{-\infty}^{\infty} x f(x) dx = \int_0^{\infty} b x e^{-bx} dx$$

$$= b \left[\frac{-x e^{-bx}}{b} \Big|_0^{\infty} + \int_0^{\infty} \frac{e^{-bx}}{b} dx \right] = b \left[\frac{e^{-bx}}{-b^2} \Big|_0^{\infty} \right]$$

$$\begin{array}{ll} \text{Let } u=x & dv=e^{-bx} dx \\ du=dx & v=-e^{-bx}/b \end{array}$$

$$\Rightarrow m = b \left[\frac{-1}{b} (e^{-\infty} - e^0) \right] = \underline{\underline{\frac{1}{b} = m}}$$

$$(c.) \sigma^2 = \bar{x^2} - (\bar{x})^2 \text{ where } \bar{x^2} = \int_{-\infty}^{\infty} x^2 b e^{-bx} dx$$

$$\text{Using Sec. A-5 } \bar{x^2} = b e^{-bx} \left[\frac{x^2}{-b} - \frac{2x}{b^2} - \frac{2}{b^3} \right] \Big|_0^{\infty} = -b e^0 \left(\frac{2}{b^3} \right) = \frac{2}{b^2}$$

$$\Rightarrow \sigma^2 = \frac{2}{b^2} - \left(\frac{1}{b} \right)^2 = \underline{\underline{\frac{1}{b^2} = \sigma^2}}$$

B-12

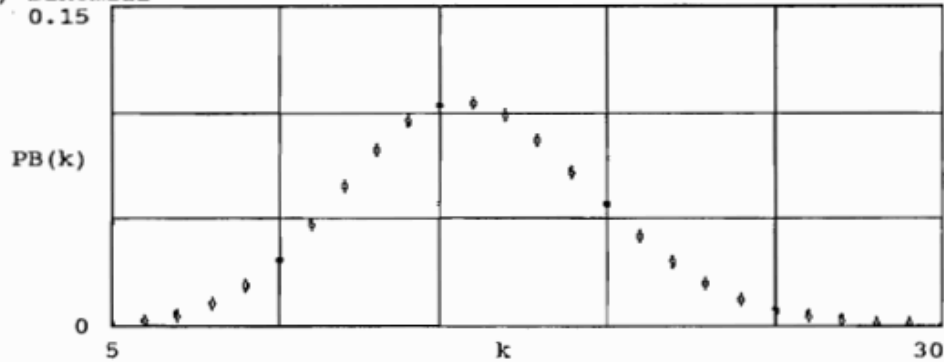
$$\begin{aligned}
 n &:= 160 & p &:= 0.1 & q &:= 1 - p & \lambda &:= n \cdot p \\
 m &:= n \cdot p & \sigma &:= \sqrt{n \cdot p \cdot q} & k &:= 0 \dots 2 \lambda & m &= 16
 \end{aligned}$$

$$\text{PB}(k) := \frac{n!}{k! (n-k)!} p^k q^{n-k} \quad \text{Binomial}$$

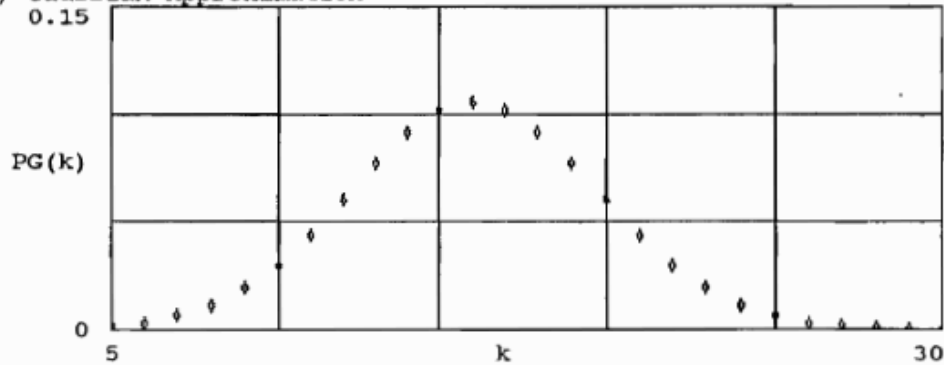
$$\text{PP}(k) := e^{-\lambda} \frac{\lambda^k}{k!} \quad \text{Poisson}$$

$$\text{PG}(k) := \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(k-m)^2}{2\sigma^2}}$$

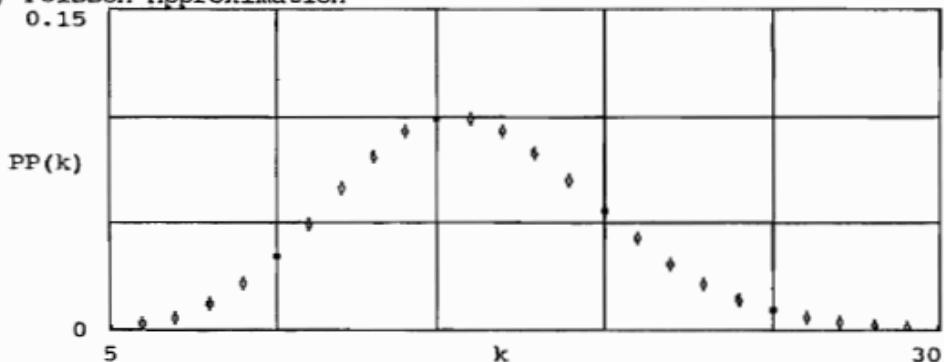
(a.) Binomial



(b.) Gaussian Approximation



(c.) Poisson Approximation



B-16

Let $f(x) = \text{pdf of } R \text{ values where}$
 $x = R \text{ value}$

$$\Rightarrow \int_{.9\bar{x}}^{1.1\bar{x}} f(x) dx \stackrel{\text{set}}{=} .95$$

$$\Rightarrow \int_{.9\bar{x}}^{1.1\bar{x}} \frac{1}{\sqrt{2\pi}\Delta} e^{-\frac{(x-\bar{x})^2}{2\Delta^2}} dx = .95$$

Let $x_1 = x - \bar{x}$; $dx_1 = dx$

$$= \int_{-.1\bar{x}}^{.1\bar{x}} \frac{1}{\sqrt{2\pi}\Delta} e^{-x_1^2/2\Delta^2} dx = .95 = 1 - 2Q\left(\frac{.1\bar{x}}{\Delta}\right)$$

$$\Rightarrow Q\left(\frac{.1\bar{x}}{\Delta}\right) = \frac{1 - .95}{2} = .025 \stackrel{\text{A-10}}{\Rightarrow} \frac{.1\bar{x}}{\Delta} = 1.96$$

$$\Rightarrow \Delta = \frac{.1\bar{x}}{1.96} = \frac{(.1)(1000)}{1.96} = \underline{\underline{51.0 \text{ ohms} = \sigma}}$$

B-25

The input is $x(t) = A \sin \omega_m t$ where $A=8$.
 The output consists of a quantized sinusoid similar to that shown in Fig. 3-8b. The PDF of the output, $y(t)$, will consist of δ functions at the quantized values. Thus,

$$f(y) = \sum_{k=1}^M P_k \delta(y - y_k)$$

where $M=8$, the step size is $\delta = \frac{2A}{M} = \frac{16}{8} = 2$, and the quantized values are:

$$y_k = \frac{(2k - M - 1)\delta}{2}$$

$$P_k = \int_{y_k - \delta/2}^{y_k + \delta/2} f_x(x) dx = \int_{y_k - \delta/2}^{y_k + \delta/2} \frac{1}{\pi \sqrt{A^2 - x^2}} dx = \int_{y_k - \delta/2}^{y_k + \delta/2} \frac{1}{\pi \sqrt{1 - (x/A)^2}} dx$$

(Using (B-67))

$$= \frac{1}{\pi} \sin^{-1}\left(\frac{x}{A}\right) \Big|_{y_k - \delta/2}^{y_k + \delta/2} = \frac{1}{\pi} \left[\sin^{-1}\left(\frac{y_k + \delta/2}{A}\right) - \sin^{-1}\left(\frac{y_k - \delta/2}{A}\right) \right]$$

or

$$P_k = \frac{1}{\pi} \left[\sin^{-1}\left(\frac{(2k - M - 1)\delta}{2A}\right) - \sin^{-1}\left(\frac{(2k - M - 1)\delta}{2A}\right) \right]$$

(Using (A-29))

$$P_k = \frac{1}{\pi} \left[\sin^{-1}\left(\frac{(2k - M)\frac{2A}{M}}{2A}\right) - \sin^{-1}\left(\frac{(2k - M - 2)\frac{2A}{M}}{2A}\right) \right] = \frac{1}{\pi} \left[\sin^{-1}\left(\frac{2k - M}{M}\right) - \sin^{-1}\left(\frac{2k - M - 2}{M}\right) \right]$$

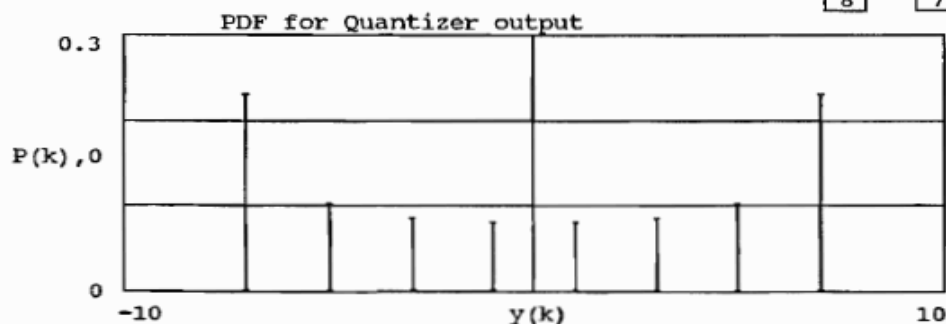
$$A := 8 \quad M := 8 \quad \delta := 2 \frac{A}{M} \quad \delta = 2 \quad \leftarrow \text{Step size}$$

$$k := 1 \dots M$$

$$y(k) := (2k - M - 1) 0.5 \cdot \delta$$

$$P(k) := \frac{1}{\pi} \left[\text{asin}\left[\frac{2 \cdot k - M}{M}\right] - \text{asin}\left[\frac{2 \cdot k - M - 2}{M}\right] \right]$$

k	y(k)
1	-7
2	-5
3	-3
4	-1
5	1
6	3
7	5
8	7



B-27

$$\begin{aligned}
 \bar{y} &= \int_{-\infty}^{\infty} y f(y) dy = \int_{-\infty}^{\infty} \frac{y}{\sqrt{2\pi} B\Delta} e^{-y^2/2B^2\Delta^2} dy \\
 &\quad + \frac{1}{2} \int_{-\infty}^{\infty} y \delta(y) dy \\
 &= \left(\frac{-B\Delta}{\sqrt{2\pi}} \right) \int_{-\infty}^{\infty} e^{-y^2/2B^2\Delta^2} \left(\frac{-y}{B^2\Delta^2} \right) dy \\
 &\stackrel{\uparrow}{=} \left(\frac{-B\Delta}{\sqrt{2\pi}} \right) \int_{-\infty}^{\infty} e^z dz = \left(\frac{-B\Delta}{\sqrt{2\pi}} \right) e^z \Big|_{-\infty}^{\infty} \\
 &\quad \text{Let } z = \frac{-y^2}{2B^2\Delta^2} \\
 &\quad dz = \frac{-y}{B^2\Delta^2} dy \\
 &= \frac{B\Delta}{\sqrt{2\pi}} = \bar{y}
 \end{aligned}$$

B-34

$$\begin{aligned}
 \mathbf{m}_x &:= \begin{bmatrix} 2 \\ -1 \end{bmatrix} & \mathbf{C}_x &:= \begin{bmatrix} & -2 \\ 5 & \sqrt{5} \\ -2 & \\ \sqrt{5} & 4 \end{bmatrix} & \mathbf{T} &:= \begin{bmatrix} & 1 \\ 1 & - \\ 1 & 2 \\ 2 & 1 \end{bmatrix} \\
 \text{(a.) Compute the mean vector for } \mathbf{y}: & & & & & \\
 \mathbf{m}_y &:= \mathbf{T} \mathbf{m}_x & & & & \mathbf{m}_y = \underline{\underline{\begin{bmatrix} 1.5 \\ 0 \end{bmatrix}}} \\
 \text{(b.) Compute the covariance matrix, } \mathbf{C}_y: & & & & & \\
 \mathbf{C}_y &:= \mathbf{T} \cdot \mathbf{C}_x \cdot \mathbf{T}^T & & & & \mathbf{C}_y = \underline{\underline{\begin{bmatrix} 5.106 & 3.382 \\ 3.382 & 4.356 \end{bmatrix}}}
 \end{aligned}$$

B-34 (Continued)

(c.) Compute the correlation coefficient for y_1 and y_2 :

$$\rho := \frac{c_{y_{0,1}}}{\left[\sqrt{c_{y_{0,0}}} \right] \left[\sqrt{c_{y_{1,1}}} \right]} \quad \underline{\underline{\rho = 0.717}}$$



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