

## Chapter 3

### 3-3

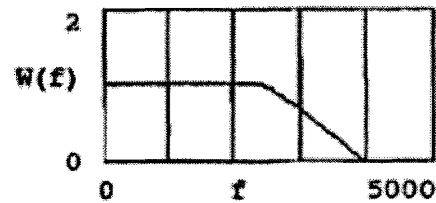
A := 1      f1 := 2500      f2 := 4000

f := 0,200 ..5000

W1(x) := if(|x| < f1,A,0)

W2(x) :=  $\left[ \frac{-A}{f2 - f1} \right] \cdot (|x| - f2) \cdot (\phi(|x| - f1) - \phi(|x| - f2))$

W(x) := W1(x) + W2(x)



fs := 10000

r := 50 10<sup>-6</sup>

Ts :=  $\frac{1}{fs}$

d :=  $\frac{r}{Ts}$

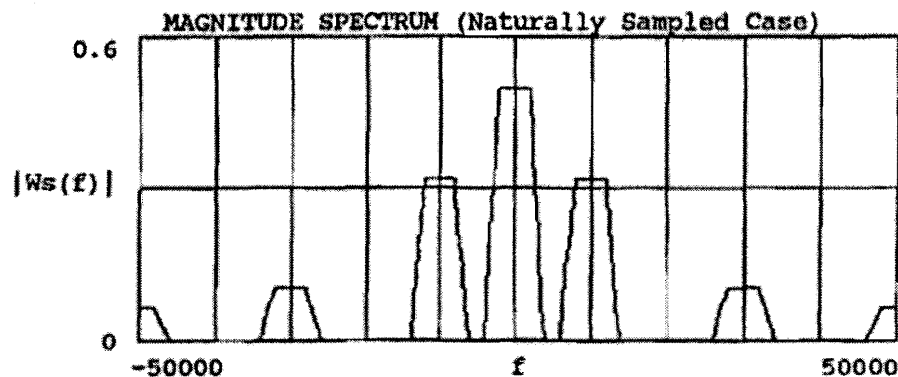
Naturally-sampled PAM

n := -5,-4 ..5

Sa(x) := if  $\left[ x \neq 0, \frac{\sin(x)}{x}, 1 \right]$

f := -50000,-48000 ..50000

Ws(f) := d ·  $\sum_n (Sa(\pi n d)) \cdot W(f - n \cdot fs)$



3-4

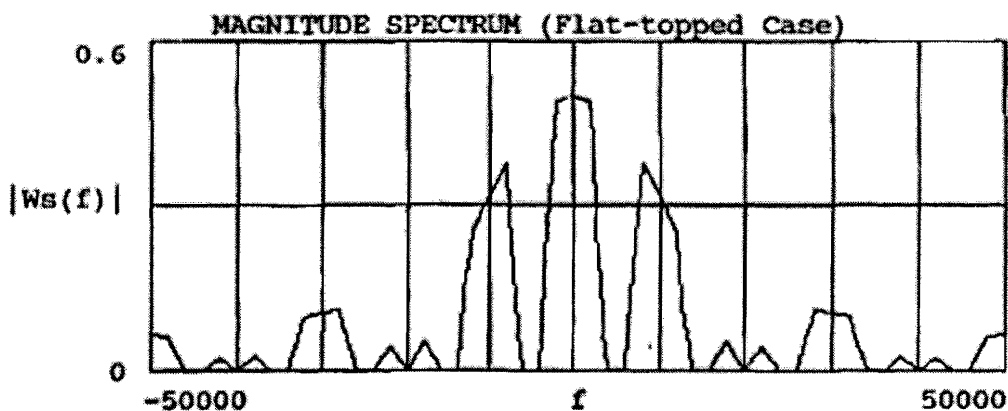
Use the parameters given in P 3-3 above.

Flat-topped PAM

$$H(f) := \tau \text{Sa}(\pi \tau f)$$

$$W_s(f) := \left[ \frac{1}{T_s} \right] \cdot H(f) \cdot \sum_n W(f - n f_s)$$

See next screen for plot



3-7

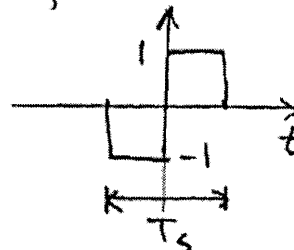
using (3-10)

$$W_s(f) = \frac{H(f)}{T_s} \sum_{k=-\infty}^{\infty} W(f - k f_s)$$

where  $H(f)$  is the spectrum of the Manchester encoded pulse,  $h(t)$ .

Thus

$$\begin{aligned} H(f) &= \int_{-\infty}^{\infty} h(t) e^{-j\omega t} dt \\ &= \int_{-T_s/2}^0 (-1) e^{-j\omega t} dt + \int_0^{T_s/2} (1) e^{-j\omega t} dt \end{aligned}$$



3-7 Cont'd.

$$= \frac{j}{\omega} \left[ -e^{-j\omega t} \Big|_{-T_s/2}^0 + e^{-j\omega t} \Big|_0^{T_s/2} \right]$$

$$= \frac{-j}{\omega} \left[ 2 - 2 \left( \frac{e^{j\omega T_s/2} + e^{-j\omega T_s/2}}{2} \right) \right] \rightarrow \cos \frac{\omega T_s}{2}$$

$$H(f) = -j T_s \frac{(1 - \cos \omega T_s/2)}{\omega T_s/2}$$

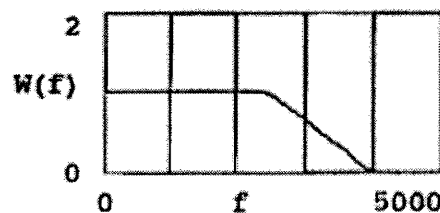
$\Lambda := 1$        $f1 := 2500$        $f2 := 4000$

$f := 0, 200 \dots 5000$

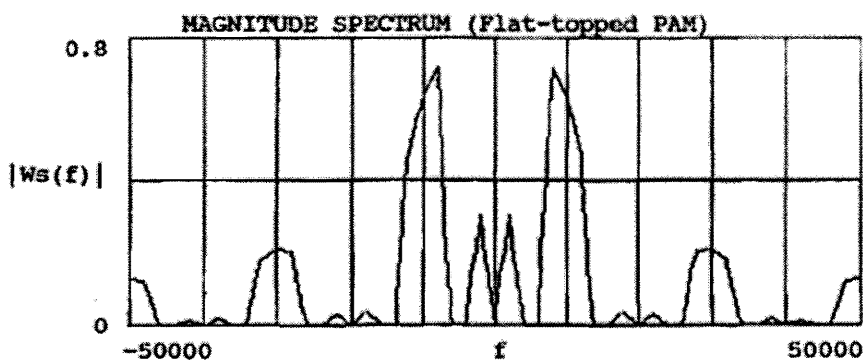
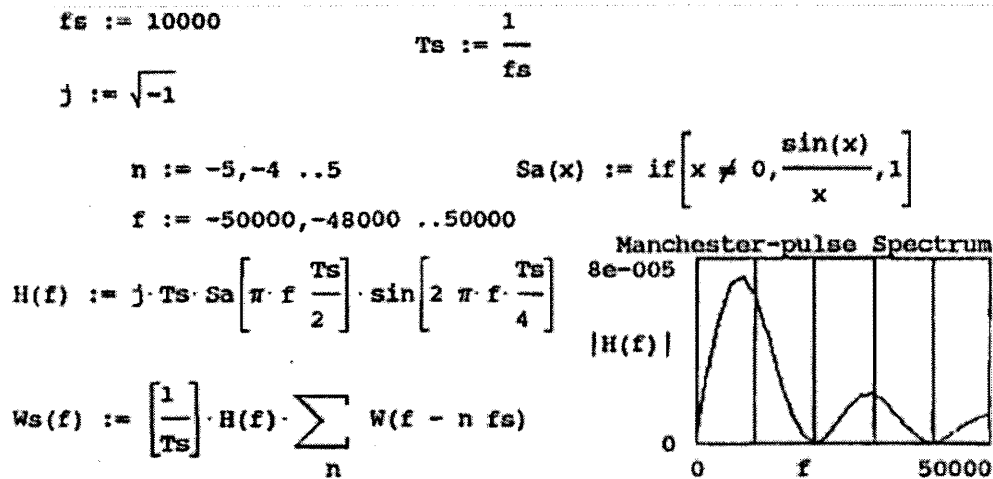
$W1(x) := \text{if}(|x| < f1, \Lambda, 0)$

$W2(x) := \left[ \frac{-\Lambda}{f2 - f1} \right] (|x| - f2) (\Phi(|x| - f1) - \Phi(|x| - f2))$

$W(x) := W1(x) + W2(x)$



3-7 Cont'd.



3-9

(a.)  $f_s = 2B = 2(100) = \underline{\underline{200 \text{ samples/sec}}}$

(b.) Using the results given in prob. 3-8.

$$n \geq 3.32 \log_{10} \left( \frac{50}{P} \right) = 3.32 \log_{10} \left( \frac{50}{0.1} \right) = 8.96$$

$$n = \underline{\underline{9 \text{ bits/word}}}$$

$$(c.) R = \left( \frac{n \text{ bits}}{\text{word}} \right) \left( \frac{f_s \text{ words}}{\text{sec}} \right) = 200(9) = \underline{\underline{1.8 \text{ Kbits/sec}}}$$

(d.) For binary PCM  $D = R$

eq. (3-74)  $D = \frac{2B}{1+r}$ , for  $B_{\min}$ ,  $r=0$

$$\Rightarrow B = \frac{D}{2} = \underline{\underline{900 \text{ Hz}}}$$

**3-12**

$$(a) f_s \geq 2 B_{\text{analog}} = 2(20 \text{ kHz}) = 40 \frac{\text{samples}}{\text{sec}}$$

For 8X oversampling of the recovered PCM signal  
(used to increase  $f_s$  8X and simplify LFF requirements)

$$\Rightarrow f_{8x} = 8 f_s = 320 \frac{\text{samples}}{\text{sec}}$$

$$B_{\text{null}} = R = n f_{8x} = \left( \frac{16 \text{ bits}}{\text{sample}} \right) \left( 320 \frac{\text{samples}}{\text{sec}} \right) = \underline{\underline{5.12 \text{ MHz}}}$$

(b) Using (3-18)

$$\left( \frac{S}{N} \right)_{\text{peak}} = 6.02n + 4.77 \text{ dB} = 6.02(5) + 4.77 = \underline{\underline{94.77 \text{ dB}}}$$

**3-16**

$$(a) P_e = 10^{-4} \quad \frac{S}{N} \geq 30 \text{ dB}$$

$$\text{Eg. (3-16)} \quad \left( \frac{S}{N} \right)_{\text{dB}} = 10 \log_{10} \left[ \frac{3m^2}{1 + 4(m^2 - 1)P_e} \right]$$

$$m = 2^n \text{ levels}$$

$$\text{for } n=4 : \left( \frac{S}{N} \right)_{\text{out}} = 28.4 \text{ dB}$$

$$\text{for } \underline{\underline{n=5}} : \left( \frac{S}{N} \right)_{\text{out}} = 33.4 \text{ dB}$$

$$\rightarrow m = 2^5 = \underline{\underline{32 \text{ levels}}}$$

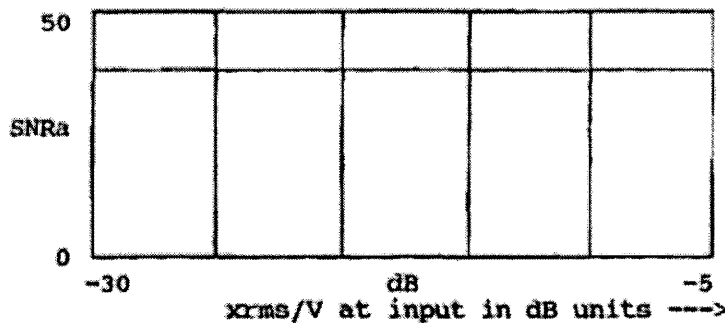
$$(b) f_s = 2(2.7 \text{ kHz}) = 5.4 \text{ k} \frac{\text{samples}}{\text{sec}}$$

The first zero-crossing of the  $\frac{\sin x}{x}$   
type spectrum is :

$$B = \frac{n}{T_s} = n f_s = 5(5.4 \text{ k}) = \underline{\underline{27 \text{ kHz} = B}}$$

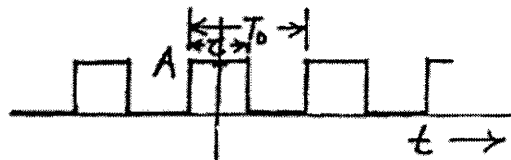
**3-20**

$$\begin{aligned} \text{dB} &:= -30, -29 \dots -5 & M &:= 256 & n &:= \frac{\log(M)}{\log(2)} \\ \mu &:= 255 & n &= 8 \\ \text{SNRa} &:= 6.02 n + 4.77 - 20 \log(\ln(1 + \mu)) \end{aligned}$$



**3-24**

For alternating data the waveform is periodic where  $T_0 = 2T_b$ .



From (2-109) the spectrum is

$$W(f) = \sum_{-\infty}^{\infty} C_n \delta(f - n f_0)$$

Where

$$\begin{aligned} C_n &= \frac{1}{T_0} \int_a^{a+T_0} w(t) e^{-jn\omega_0 t} dt = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} A e^{jn\omega_0 t} dt \\ &= \frac{A}{T_0} \left. \frac{e^{jn\omega_0 t}}{jn\omega_0} \right|_{-\frac{T_0}{2}}^{\frac{T_0}{2}} = \frac{2A}{T_0} \frac{\sin(n\omega_0 \frac{T_0}{2})}{n\omega_0} \end{aligned}$$

$$\Rightarrow C_n = \frac{2A}{T_0} \frac{\sin(n\omega_0 \frac{T_0}{2})}{n\omega_0} = \frac{A}{T_0} \left( \frac{T_0}{2} \right) \frac{\sin(\frac{n\pi}{2})}{(\frac{n\pi}{2})}$$

$$\Rightarrow W(f) = \sum_{n=-\infty}^{\infty} \frac{A}{T_0} \left( \frac{T_0}{2} \right) \left( \frac{\sin(\frac{n\pi}{2})}{(\frac{n\pi}{2})} \right) \delta(f - \frac{n}{T_0}) \quad \textcircled{A}$$

where  $R = \frac{1}{T_0} = \text{bit rate}$

3-24. Cont'd

(a) Using (A) for NRZ signaling with  $\tau = T_b$ 

$$|W(f)| = \sum_{-\infty}^{\infty} \frac{A}{2} \left| \frac{\sin(\frac{n\pi}{2})}{(\frac{n\pi}{2})} \right| \delta(f - \frac{n}{2}R) \quad \begin{array}{l} \text{Unipolar} \\ \text{NRZ} \\ \text{(alternating} \\ \text{data)} \end{array}$$

If the data are a sequence of four "1"s followed by four "0"s, the waveform would have the same shape except  $T_0$  would be 4 times as large.

i.e.  $T_0 = 8T_b$ .

$$\Rightarrow |W(f)| = \sum_{-\infty}^{\infty} \frac{A}{2} \left| \frac{\sin(\frac{n\pi}{2})}{(\frac{n\pi}{2})} \right| \delta(f - \frac{n}{8}R) \quad \begin{array}{l} \text{Unipolar NRZ} \\ \text{4 '1's and 4 '0's'} \end{array}$$

**3-25**Using (A) for RZ signaling with  $\tau = \frac{3}{4}T_b$ 

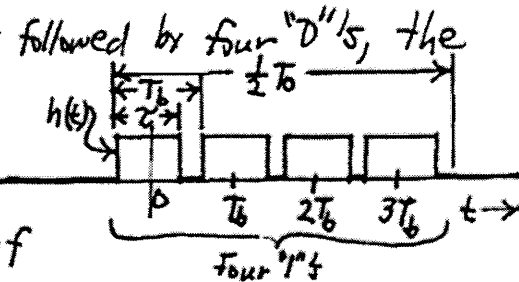
$$|W(f)| = \sum_{-\infty}^{\infty} \frac{3A}{8} \left| \frac{\sin(\frac{3}{8}n\pi)}{(\frac{3}{8}n\pi)} \right| \delta(f - \frac{n}{2}R) \quad \begin{array}{l} \text{Unipolar RZ} \\ \text{(alternating data)} \end{array}$$

For RZ with four "1"s followed by four "0"s, the periodic waveform would appear as shown where  $T_0 = 8T_b$ . The mathematical calculations are simplified if (2-112) is used

$$C_h = f_0 H(nf_0)$$

where  $h(t)$  is the basic waveform that is repeated to create the periodic waveform (as shown in the figure).

$h(t)$  consists of the superposition of four rectangular pulses. Using the time delay theorem of Table 2-1



3-25 Cont'd.

and the rectangular pulse spectrum of Table 2-2

$$H(f) = Az \frac{\sin(\pi f z)}{\pi f z} [1 + e^{-j\omega T_b} + e^{-j\omega 2T_b} + e^{-j\omega 3T_b}]$$

$$\text{Or } c_n = \frac{Az}{8T_b} \frac{\sin\left(\frac{n\pi}{8} \frac{z}{T_b}\right)}{\left(\frac{n\pi}{8} \frac{z}{T_b}\right)} [1 + e^{-j\frac{n\pi}{4}} + e^{-j\frac{n\pi}{2}} + e^{-j\frac{3n\pi}{4}}]$$

$$\boxed{f = nf_0 = \frac{n}{T_b} = \frac{n}{8T_b}}$$

For RZ with  $z = \frac{3}{4}T_b$ , this becomes

$$c_n = \frac{3}{32} A \left( \frac{\sin\left(\frac{3}{32} n\pi\right)}{\left(\frac{3}{32} n\pi\right)} \right) [1 + e^{-j\frac{n\pi}{4}} + e^{-j\frac{n\pi}{2}} + e^{-j\frac{3n\pi}{4}}]$$

Thus, the spectrum for Unipolar RZ with four alternate "1" and "0"s is

$$|W(f)| = \sum_{n=-\infty}^{\infty} \frac{3}{32} A \left| \frac{\sin\left(\frac{3}{32} n\pi\right)}{\left(\frac{3}{32} n\pi\right)} \right| |1 + e^{-j\frac{n\pi}{4}} + e^{-j\frac{n\pi}{2}} + e^{-j\frac{3n\pi}{4}}| \delta\left(f - \frac{n}{8T_b}\right)$$

**3-29**

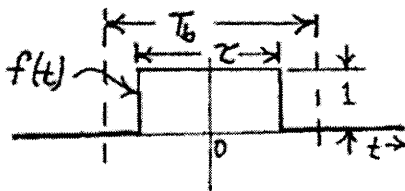
(a) Substituting (3-40) into (3-36a) the PSD for Polar RZ signaling is

$$P(f) = \frac{A^2}{T_b} |F(f)|^2$$

where the pulse shape,  $f(t)$ , is shown in the figure. Thus,

$$F(f) = \mathcal{F}[f(t)] = z \frac{\sin(\pi f z)}{\pi f z}$$

$$\text{and } P(f) = \frac{A^2 z^2}{T_b} \left[ \frac{\sin(\pi f z)}{\pi f z} \right]^2$$





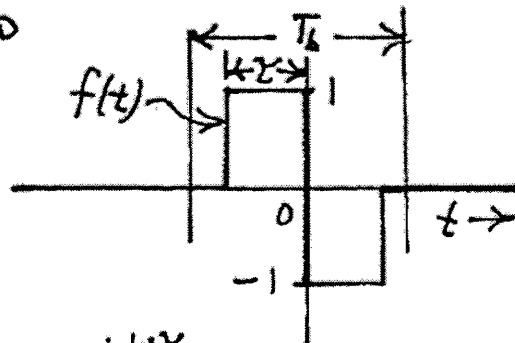
3-29 Cont'd.

For the case of  $\tau = \frac{1}{2} T_b$ , this becomes

$$\underline{\underline{P(f) = \frac{A^2 T_b}{4} \left[ \frac{\sin(\frac{\pi}{2} f T_b)}{(\frac{\pi}{2} f T_b)} \right]^2}}$$

The first-null bandwidth is  $B_{null} = \frac{2}{T_b} = 2R$   
and the bandwidth efficiency is  $\eta = \frac{1}{2}$  (bit/sec)/Hz.

(b) Equation (3-36) can also be used to evaluate the PSD for RZ Manchester signaling where the pulse shape is shown in the figure:



$$F(f) = \tau \left( \frac{\sin(\pi f \tau)}{\pi f \tau} \right) \left[ e^{j \omega \frac{\tau}{2}} - e^{-j \omega \frac{\tau}{2}} \right]$$

$$\Rightarrow F(f) = j 2 \tau \left( \frac{\sin(\pi f \tau)}{\pi f \tau} \right) \sin\left(\frac{\omega \tau}{2}\right)$$

Using (3-40) and (3-36), the PSD for Manchester signaling is

$$P(f) = \frac{4 A^2 \tau^2}{T_b} \left[ \frac{\sin(\pi f \tau)}{\pi f \tau} \right]^2 [\sin(\pi f \tau)]^2$$

If  $\tau = \frac{1}{4} T_b$ , this becomes

$$\underline{\underline{P(f) = \frac{1}{4} A^2 T_b \left[ \frac{\sin(\frac{\pi}{4} f T_b)}{(\frac{\pi}{4} f T_b)} \right]^2 [\sin(\frac{\pi}{4} f T_b)]^2}}$$

The first-null bandwidth is  $B_{null} = \frac{4}{T_b} = 4R$   
and the spectral efficiency is  $\eta = \frac{1}{4}$  (bits/sec)/Hz.

**3-31**

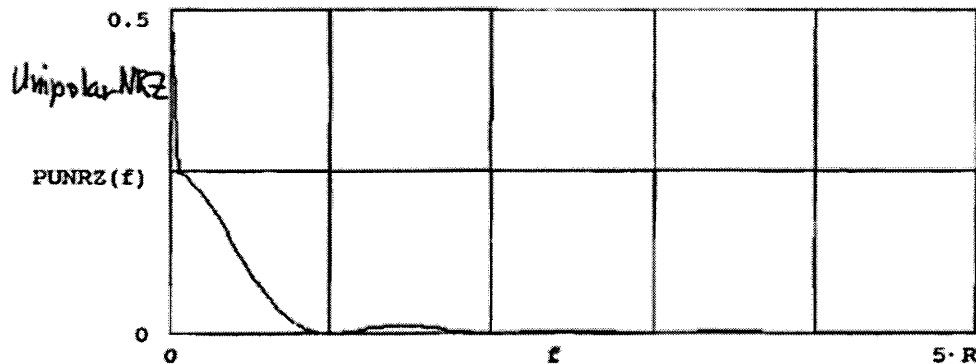
$$A := 1 \quad R := 1 \quad f := 0, 0.05 \dots 5 \quad T_b := \frac{1}{R}$$

$$Sa(x) := \text{if} \left[ x \neq 0, \frac{\sin(x)}{x}, 1 \right]$$

The PSD for Unipolar NRZ is given by (3-39b) and consists of both a continuous spectrum and a discrete spectrum. The computer cannot plot infinite values for the delta functions, so plot the weights of the delta functions instead. Thus (3-39b) will be broken into two functions, one for the continuous spectral plot and one for the discrete spectral plot.

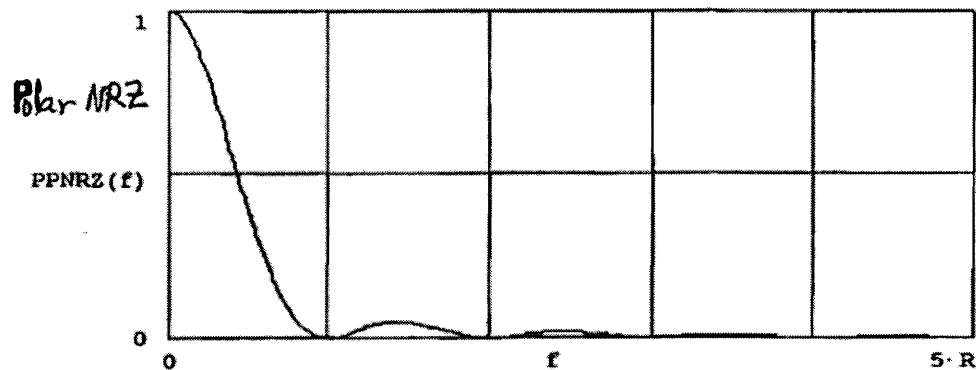
$$PUNRZc(f) := \left[ A \frac{2 T_b}{4} \right] (Sa(\pi f T_b))^2 \quad PUNRZd(f) := \text{if} \left[ f \neq 0, 0, \frac{A^2}{4} \right]$$

$$PUNRZ(f) := PUNRZc(f) + PUNRZd(f)$$



Use (3-41) for Polar NRZ spectrum:

$$PPNRZ(f) := \left[ A T_b \right] (Sa(\pi f T_b))^2$$



The PSD for Unipolar RZ is given by (3-43) and consists of both a continuous spectrum and a discrete spectrum. The computer cannot plot infinite values for the delta functions, so plot the weights of the delta functions instead. Thus (3-43) will be broken into two functions, one for the continuous spectral plot and one for the discrete spectral plot.

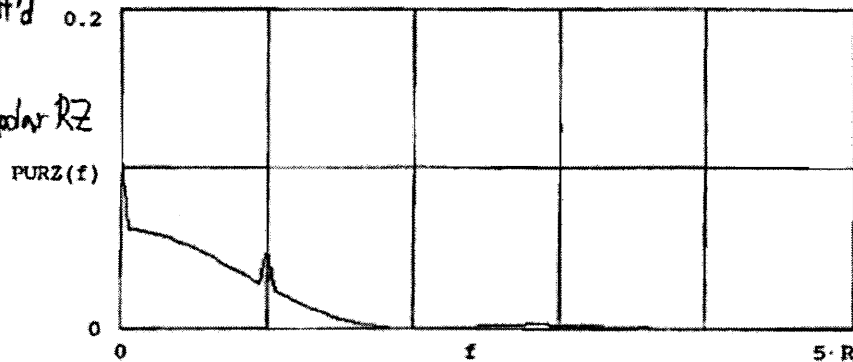
$$PURZc(f) := \left[ A \frac{2 T_b}{16} \right] \left[ Sa \left[ \pi f \frac{T_b}{2} \right] \right]^2$$

$$PURZd(f) := \text{if} \left[ \text{mod}(f, R) \neq 0, 0, \frac{A^2}{16} \left[ Sa \left[ \pi f \frac{T_b}{2} \right] \right]^2 \right]$$

3-31  $PURZ(f) := PURZc(f) + PURZd(f)$

Cont'd

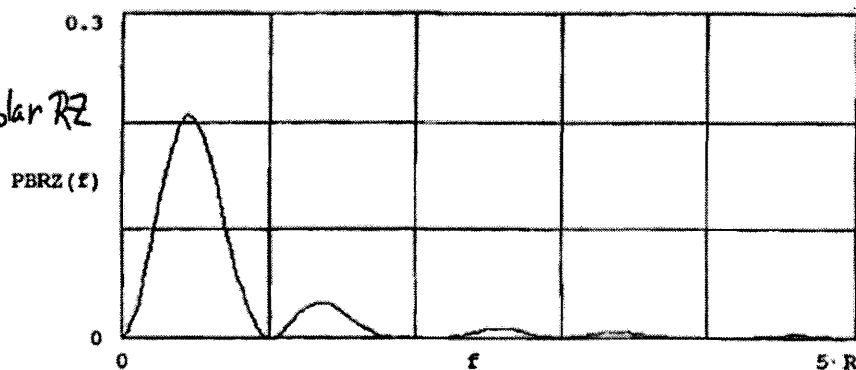
Unipolar RZ



Using (3-45) the PSD for Bipolar RZ is:

$$PBRZ(f) := A^2 \left[ \frac{T_b}{4} \right]^2 \left[ \text{Sa} \left[ \pi f \frac{T_b}{2} \right] \right]^2 (\sin(\pi f T_b))^2$$

Bipolar RZ



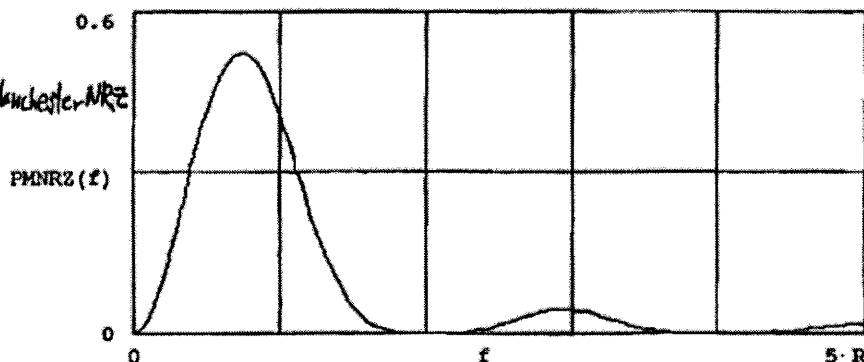
$$A := 1 \quad R := 1 \quad f := 0, 0.05 \dots 5 \quad T_b := \frac{1}{R}$$

$$\text{Sa}(x) := \text{if} \left[ x \neq 0, \frac{\sin(x)}{x}, 1 \right]$$

Use (3-46c) for the Manchester NRZ spectrum:

$$PMNRZ(f) := A^2 \cdot T_b \left[ \text{Sa} \left[ \pi f \frac{T_b}{2} \right] \right]^2 \cdot \left[ \sin \left[ \pi f \frac{T_b}{2} \right] \right]^2$$

Manchester-NRZ



**3-39** Use the result from Prob 3-8.

(a)  $n \geq 3.32 \log_{10} \left( \frac{50}{\rho} \right) = 3.32 \log_{10} (50) = 5.64 \Rightarrow$  Use  $n=6$  bits/symbol.

$f_s = 2B = 5.4 \text{ kHz} \Rightarrow R_{\text{min}} = n f_s = 6(5.4 \text{ kHz}) = \underline{\underline{32.4 \text{ kbits/sec}}}$

(b)  $L=B=2^l \Rightarrow l=36 \text{ bit/D/A} \quad D = \frac{R}{l} = \frac{32.4 \text{ kbit/sec}}{36 \text{ bits/symbol}} = \underline{\underline{0.8 \text{ ksym/sec}}}$

(c)  $D = \frac{2B}{1+r}$  where  $r=D$  for min BW  $\Rightarrow B = \frac{D}{2} = \underline{\underline{5.4 \text{ kHz}}}$

**3-40**  $L=B=2^l \Rightarrow l=3$

(a)  $D = \frac{R}{l} = \frac{9600 \text{ bits/sec}}{3 \text{ bits/symbol}} = \underline{\underline{3.2 \text{ ksymbol/sec}}}$

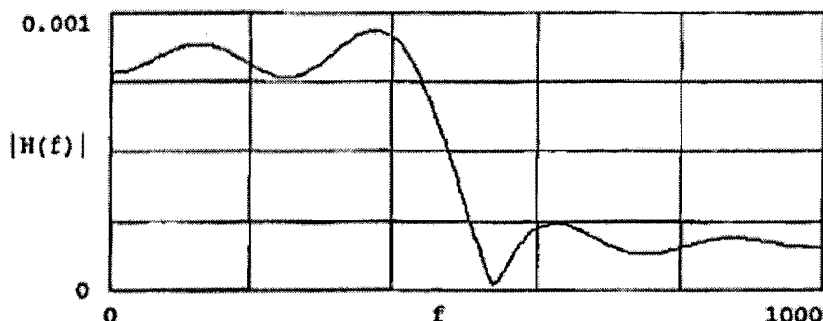
(b)  $D = \frac{2R}{1+r} = \frac{2(3.2 \text{ k})}{1+r} = 3.2 \text{ k} \Rightarrow \underline{\underline{r=0.5}}$

**3-43** (a.)

$f := 0, 10 \dots 1000$

$f_s := 1000$

$$H(f) := \int_0^{0.008} \frac{\sin(\pi f_s (t - 0.004))}{\pi f_s (t - 0.004)} e^{-2j\pi f t} dt$$



(b.) From the figure above, the bandwidth for the causal approximation is  $\underline{\underline{B=540 \text{ Hz}}}$

The bandwidth for the noncausal filter is  $\underline{\underline{B=\frac{1}{2}f_s=500 \text{ Hz}}}$

**3-47**

$$h_e(t) = \int_{-\infty}^{\infty} H_e(f) e^{j2\pi ft} df$$

$$\text{For } t = nT_s \Rightarrow h_e(nT_s) = \int_{-\infty}^{\infty} H_e(f) e^{j2\pi nT_s f} df$$

Break into multiple integrals, each with a  $\frac{1}{T_s}$  wide interval.

$$\Rightarrow h_e(nT_s) = \sum_{k=-\infty}^{\infty} \int_{-\frac{1}{2T_s} + \frac{k}{T_s}}^{\frac{1}{2T_s} + \frac{k}{T_s}} H_e(f) e^{j2\pi nT_s f} df$$

$$\text{Let } f_1 = f - \frac{k}{T_s}$$

$$\text{Then } h_e(nT_s) = \sum_{k=-\infty}^{\infty} \int_{-\frac{1}{2T_s}}^{\frac{1}{2T_s}} H_e(f_1 + \frac{k}{T_s}) e^{j2\pi nT_s (f_1 + \frac{k}{T_s})} df_1$$

$$\text{or } h_e(nT_s) = \int_{-\frac{1}{2T_s}}^{\frac{1}{2T_s}} \sum_{k=-\infty}^{\infty} H_e(f_1 + \frac{k}{T_s}) e^{j2\pi nT_s f_1} df_1$$

$$\text{Assume } \sum_{k=-\infty}^{\infty} H_e(f_1 + \frac{k}{T_s}) = T_s, \quad |f_1| < \frac{1}{2T_s}$$

$$\text{Then } h(nT_s) = \int_{-\frac{1}{2T_s}}^{\frac{1}{2T_s}} T_s e^{j2\pi nT_s f_1} df_1 = \left. \frac{T_s e^{j2\pi nT_s f_1}}{j2\pi nT_s} \right|_{-\frac{1}{2T_s}}^{\frac{1}{2T_s}}$$

$$\text{or } h(nT_s) = \frac{e^{j2\pi nT_s \frac{1}{2T_s}} - e^{-j2\pi nT_s \frac{1}{2T_s}}}{j2\pi n} = \frac{\sin(n\pi)}{n\pi} = \begin{cases} 1, & n=0 \\ 0, & n \neq 0 \end{cases}$$

Q.E.D.

3-50

$$M = 16 = 2^4 \Rightarrow h = 4$$

(a) Binary PCM  $\Rightarrow l = 1$ ,  $R = n f_s = 4 f_s = D$

$$D = \frac{2B}{1+r} = \frac{2(4 \text{ kHz})}{1+0.5} = \underline{\underline{5.33 \text{ kbits/sec}}}$$

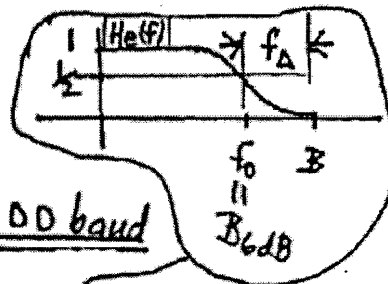
(b) From (a)  $f_s = \frac{D}{4} = \frac{5.33 \text{ k}}{4} = 1.33 \text{ kHz}$

$$B_{\text{analog max}} = \frac{f_s}{2} = \frac{1.33 \text{ k}}{2} = \underline{\underline{667 \text{ Hz}}}$$

3-52

(a)  $L = 2^l = 4 \Rightarrow l = 2$

$$D = R/l = \frac{2400}{2} = \underline{\underline{1200 \text{ baud}}}$$



(b)  $B = \frac{1}{2}(1+r)D$  where  $r = \frac{f_A}{f_0} = 0 \Rightarrow B = f_0 = B_{6dB}$

$$\Rightarrow B_{6dB} = \frac{1}{2}(1+0)D = \frac{1}{2}(1200) = \underline{\underline{600 \text{ Hz}}}$$

(c)

$$B_{\text{absolute}} = \frac{1}{2}(1+r)D = \frac{1}{2}(1+0.5)(1200) = \frac{3}{4}(1200)$$

$r = 0.5$

$$\Rightarrow \underline{\underline{B_{\text{absolute}} = 900 \text{ Hz}}}$$

**3-59**

(a.) From (3-84)

$$\delta = \frac{2\pi f_a A}{f_s} ; f_a = 3.4 \text{ kHz} \ \& \ A = \frac{1}{2}$$

We need to determine the  $f_s$  which the channel can support. Assuming that a  $r=0$  roll-off factor is used, then

$$f_s = B = 2B = 2(1 \text{ MHz}) = 2 \times 10^6 \frac{\text{Samples}}{\text{Sec}}$$

$$\Rightarrow \delta = \frac{2\pi (3.4 \text{ k}) (\frac{1}{2})}{2 \times 10^6} = \underline{\underline{0.00534}}$$

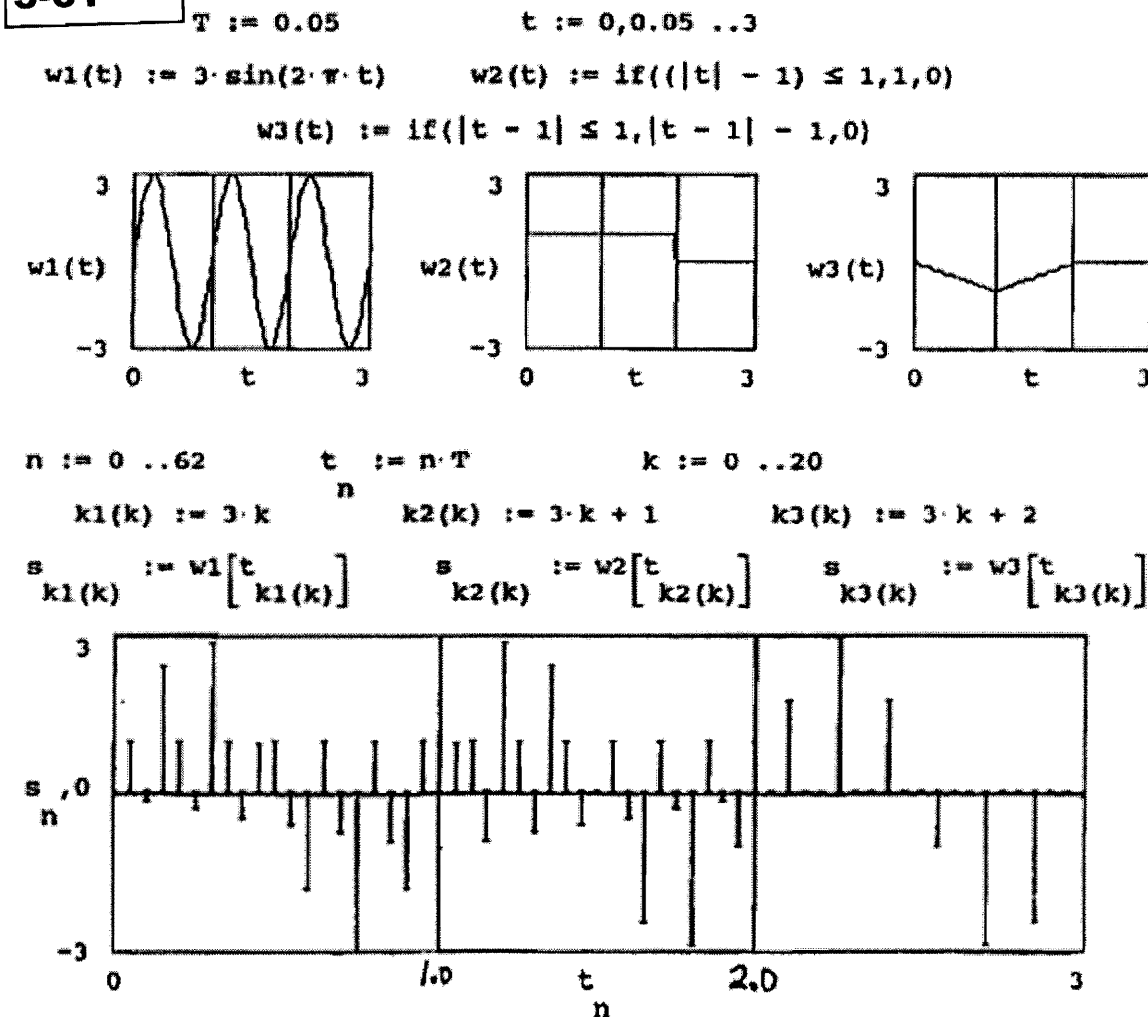
(Note: The channel has to be equalized with a Nyquist filter.)

(b.)

$$\delta = \frac{2\pi (3.4 \text{ k}) (\frac{1}{2})}{25 \times 10^3} = \underline{\underline{0.427}}$$

(Note: No Channel equalization required.)

**3-61**

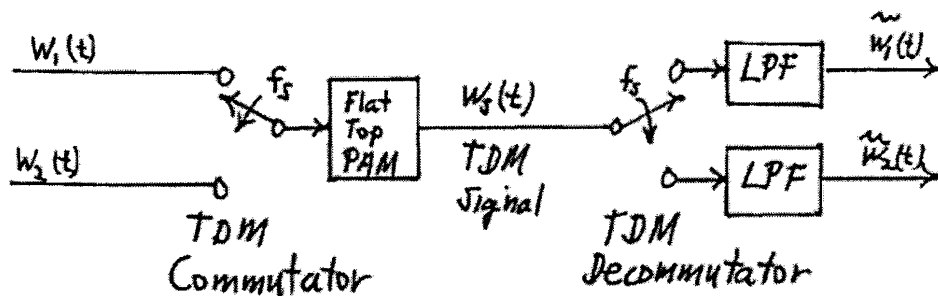


**3-63** (a) Each analog signal has a highest frequency of  $B = 3 \text{ kHz}$

⇒ The minimum sampling frequency for each analog signal is  $f_s = 2B = 6 \text{ kHz}$



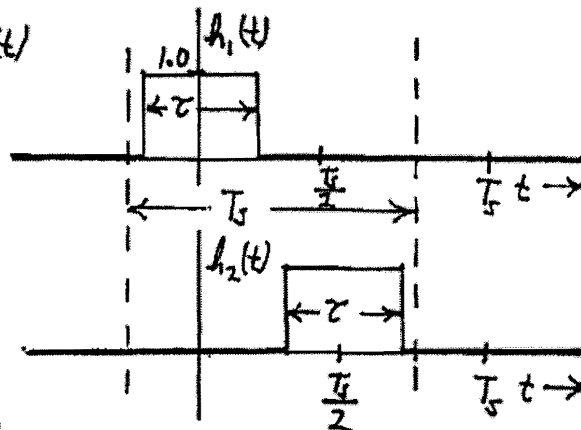
3-63.(a.) Cont'd



(b) Referring to (3-8), the sampled TDM signal is

$$w_s(t) = \sum_{k=-\infty}^{\infty} w_1(kT_s) h_1(t - kT_s) + \sum_{k=-\infty}^{\infty} w_2(kT_s) h_2(t - kT_s)$$

where  $h_1(t)$  and  $h_2(t)$  are shown in the figure and  $\tau \leq \frac{T_s}{2}$  and  $f_s \geq 2B$ .



Following the same procedure as described in (3-8) thru (3-13), the spectrum of the TDM instantaneously sampled (flat-topped) PAM signal is

$$W_s(f) = \frac{1}{T_s} H_1(f) \sum_{k=-\infty}^{\infty} W_1(f - kf_s) + \frac{1}{T_s} H_2(f) \sum_{k=-\infty}^{\infty} W_2(f - kf_s)$$

where  $H_1(f) = \tau \left( \frac{\sin(\pi f \tau)}{\pi f \tau} \right)$  and  $H_2(f) = \tau \left( \frac{\sin(\pi f \tau)}{\pi f \tau} \right) e^{-j2\pi f \frac{T_s}{2}}$

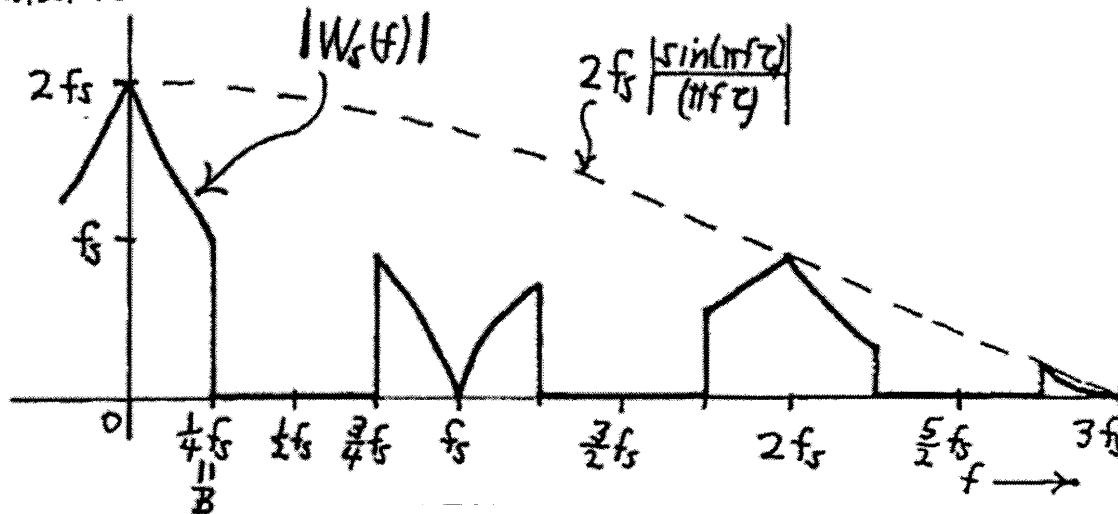
$$\Rightarrow W_s(f) = f_s \tau \frac{\sin(\pi f \tau)}{\pi f \tau} \sum_{k=-\infty}^{\infty} \Pi\left(\frac{f - kf_s}{2B}\right) + 2B\tau \left( \frac{\sin(\pi f \tau)}{(\pi f \tau)} \right) + 2B\tau \left( \frac{\sin(\pi f \tau)}{(\pi f \tau)} \right) e^{j\pi T_s f} \sum_{k=-\infty}^{\infty} \Lambda\left(\frac{f - kf_s}{B}\right)$$

### 3-63 (b.) Cont'd

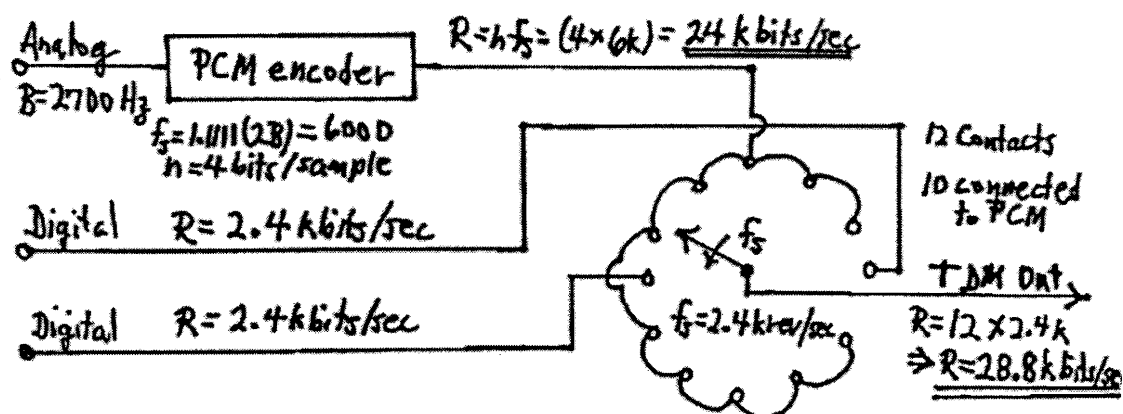
Thus,

$$|W_s(f)| = f_s \left| \frac{\sin(\pi f \tau)}{(\pi f \tau)} \right| \sum_{k=-\infty}^{\infty} \left| \Pi\left(\frac{f - k f_s}{2B}\right) + e^{j\pi f_s \tau} \Pi\left(\frac{f - k f_s}{B}\right) \right|$$

For the sketch, let the parameters be the same as those shown in Fig. 3-6. Let  $\tau/T_s = 1/3$ ,  $f_s = 4B$ . Using a programmable calculator, the following sketch is obtained.



### 3-66



**3-70**

(a) For PCM a  $N=8$  dimensional system is used since any of the 256 messages can be represented

by 
$$s_i(t) = \sum_{j=1}^8 s_{ij} \phi_j(t)$$

where  $s_{ij} = \pm 1$  for binary PCM.

$$T_0 = \frac{1}{10 \text{ mess/sec.}} = \underline{\underline{0.1 \text{ sec/message}}}$$

$$B = \frac{1}{2} \left( \frac{N}{T_0} \right) = \frac{1}{2} \left( \frac{8}{0.1} \right) = \underline{\underline{40 \text{ Hz}}}$$

(b) For PPM a  $N=256$  dimensional system is used:

$$s_i(t) = \sum_{j=1}^{256} s_{ij} \phi_j(t) \quad \text{where } s_{ij} = \pm 1$$

$$B = \frac{1}{2} \left( \frac{N}{T_0} \right) = \frac{1}{2} \left( \frac{256}{0.1} \right) = \underline{\underline{1,280 \text{ Hz}}}$$